

# Multi-objective linear optimization for strategic planning of shared autonomous vehicle operation and infrastructure design

Toru Seo\* and Yasuo Asakura

\*Assoc. Prof., Tokyo Institute of Technology

seo.t.aa@m.titech.ac.jp

DTA2021



Tokyo Tech

\*This work has been published in the DTA special issue  
in IEEE Transactions on ITS

<http://dx.doi.org/10.1109/TITS.2021.3071512>



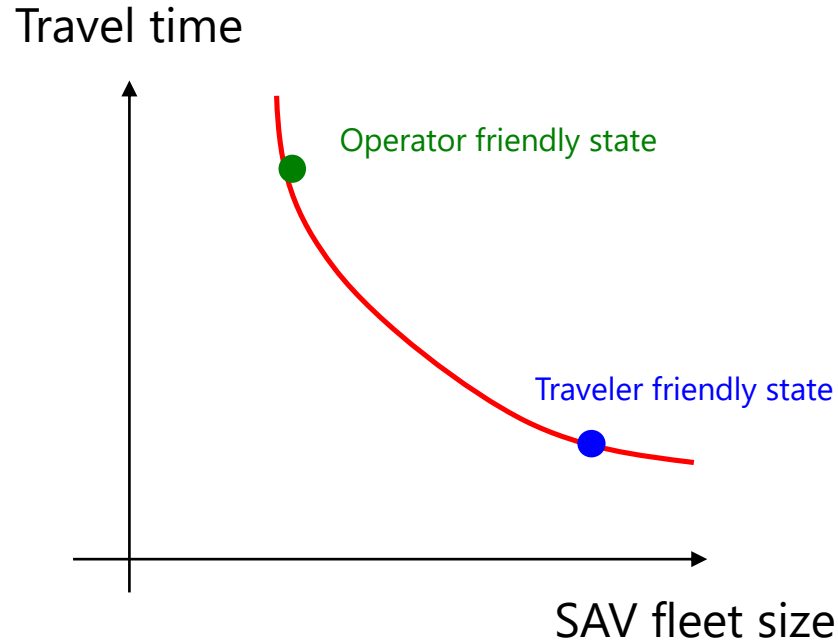
## Strategic planning of SAV systems

- Network design
- Parking slot allocation
- Fleet size

## Operational planning of SAV systems

- SAV routing
- Passenger pickup/drop-off
- Ridesharing

Unified, tractable DTA framework for strategic optimization with explicit consideration to operation



- Trade-offs between objective values

Travel time  $\longleftrightarrow$  SAV fleet size

Traveler utility  $\longleftrightarrow$  Operator benefit

Profit-seeking operator  $\longleftrightarrow$  Public sector operator

- It is important to clarify the trade-off relations before implementing SAV systems

Multi-objective optimization to explicitly consider and derive trade-offs

- Dynamic OD matrix of travelers is available
- The only transportation mode is an SAV system
- Each SAV has passenger capacity
- Each road has traffic capacity
- Each node has storage capacity (queuing, parking)

Problem: Find the optimal SAV and passenger flow and infrastructure design that satisfy the traveler demand under the capacity constraints

# Model: Multi-objective optimization problem

[SOSAV]  $\min(T, D, N, C)$

subject to

$$\sum_{ij,s,t,k} t_{ij} y_{s,ij}^{k,t} = T$$

$$\sum_{ij,i \neq j} d_{ij} x_{ij}^t = D$$

$$\sum_i x_{0i}^0 = N$$

$$\sum_{ij} c_{ij} (\mu_{ij} - \mu_{ij}^{\min}) + \sum_i c_i (\kappa_i - \kappa_i^{\min}) = C$$

definition of objective values

$$\sum_j x_{ji}^{t-t_{ji}} - \sum_j x_{ij}^t = 0 \quad \forall i, t \in (0, t_{\max})$$

conservation law of SAVs

$$\sum_j y_{s,ji}^{k,t-t_{ji}} - \sum_j y_{s,ij}^{k,t} + y_{s,0i}^{k,t} - y_{s,i0}^{k,t} = 0 \quad \forall i, s, k, t \in T_k$$

$$\sum_{s,k} y_{s,ij}^{k,t} \leq \rho x_{ij}^t \quad \forall ij, i \neq j, t$$

conservation law of passengers

$$x_{ij}^t \leq \mu_{ij} \quad \forall ij, i \neq j, t$$

link capacity

$$x_{ii}^t \leq \kappa_i \quad \forall i, t$$

parking capacity

$$y_{s,0r}^{k,k} = M_{rs}^k \quad \forall rs, k$$

$$\sum_{t \in T_k} y_{s,s0}^{k,t} = \sum_r M_{rs}^k \quad \forall s, k$$

passengers' departure and arrival time

$$x_{ij}^t \geq 0 \quad \forall ij, t$$

$$y_{s,ij}^{k,t} \geq 0 \quad \forall ij, s, k, t \in T_k$$

$$x_{0i}^0 \geq 0 \quad \forall i$$

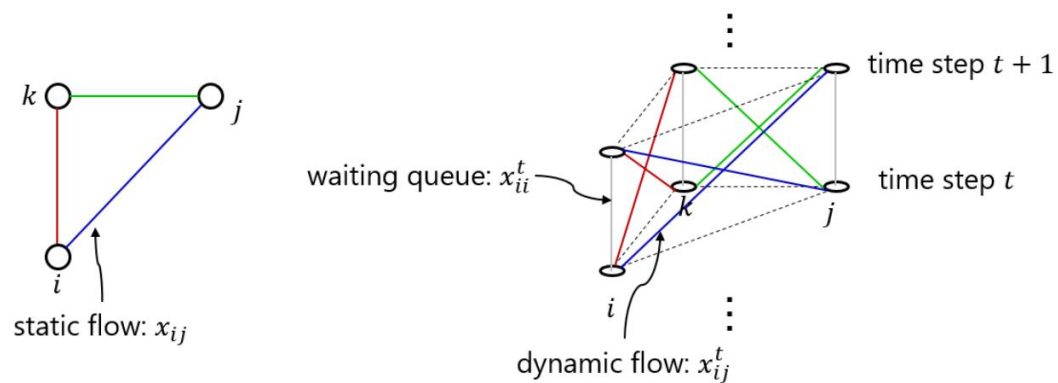
$$y_{s,s0}^{k,t} \geq 0 \quad \forall s, t, k \in T_k$$

$$\mu_{ij}^{\min} \leq \mu_{ij} \leq \mu_{ij}^{\max} \quad \forall ij$$

$$\kappa_i^{\min} \leq \kappa_i \leq \kappa_i^{\max} \quad \forall i$$

- Objective functions:
  - Total travel time of passengers
  - Total distance traveled by SAVs
  - SAV fleet size
  - Total infrastructure (road, parking) cost
  
- Key decision variables:
  - Dynamic SAV flow
  - Dynamic passenger flow
  - SAV fleet size
  - Link capacity, parking capacity
  
- Multi-objective linear programming
- Solution = Pareto frontier

# Model: Traffic features



$$\sum_j x_{ji}^{t-t_{ji}} - \sum_j x_{ij}^t = 0 \quad \forall i, t \in (0, t_{\max})$$

conservation law  
of SAVs

$$\sum_j y_{s,ji}^{k,t-t_{ji}} - \sum_j y_{s,ij}^{k,t} + y_{s,0i}^{k,t} - y_{s,i0}^{k,t} = 0 \quad \forall i, s, k, t \in T_k$$

$$\sum_{s,k} y_{s,ij}^{k,t} \leq \rho x_{ij}^t \quad \forall i, j, i \neq j, t$$

conservation law  
of passengers

$$x_{ij}^t \leq \mu_{ij} \quad \forall i, j, i \neq j, t$$

link capacity

$$x_{ii}^t \leq \kappa_i \quad \forall i, t$$

parking capacity

$$y_{s,0r}^{k,k} = M_{rs}^k \quad \forall r, s, k$$

$$\sum_{t \in T_k} y_{s,s0}^{k,t} = \sum_r M_{rs}^k \quad \forall s, k$$

passengers'  
departure and  
arrival time

$$x_{ij}^t \geq 0 \quad \forall i, j, t$$

$$y_{s,ij}^{k,t} \geq 0 \quad \forall i, j, s, k, t \in T_k$$

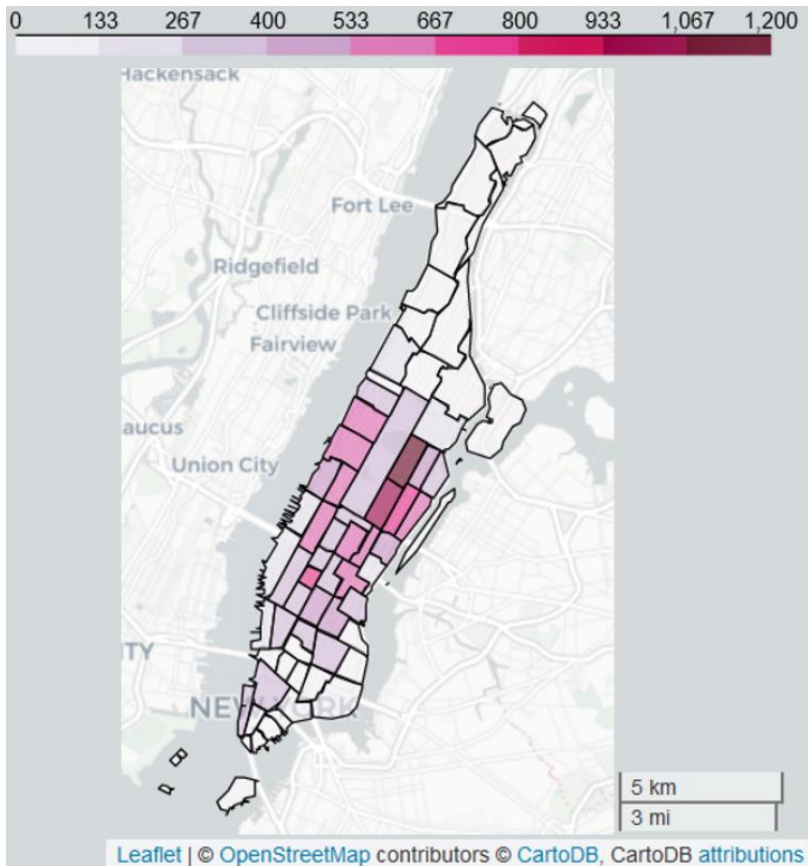
$$x_{0i}^0 \geq 0 \quad \forall i$$

$$y_{s,s0}^{k,t} \geq 0 \quad \forall s, t, k \in T_k$$

$$\mu_{ij}^{\min} \leq \mu_{ij} \leq \mu_{ij}^{\max} \quad \forall i, j$$

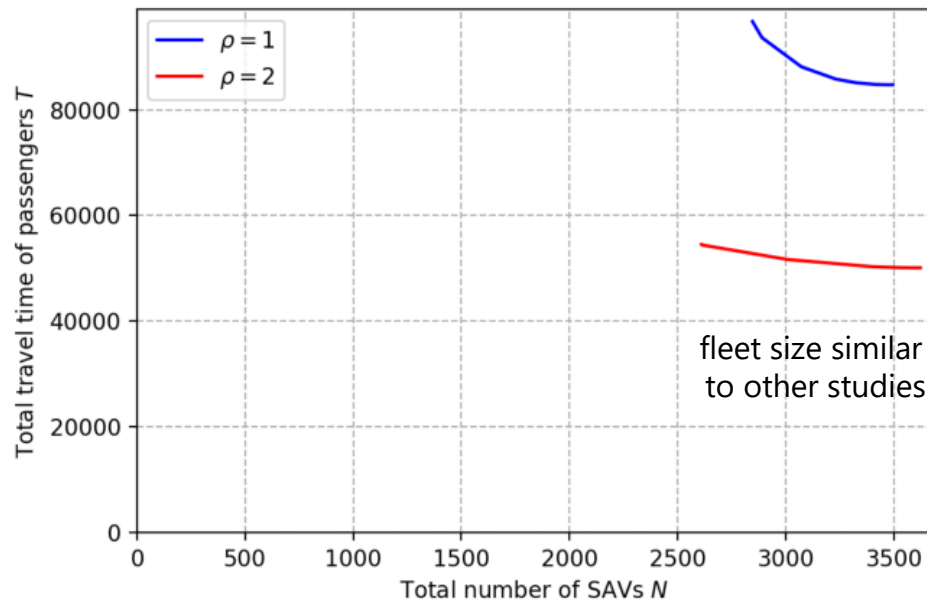
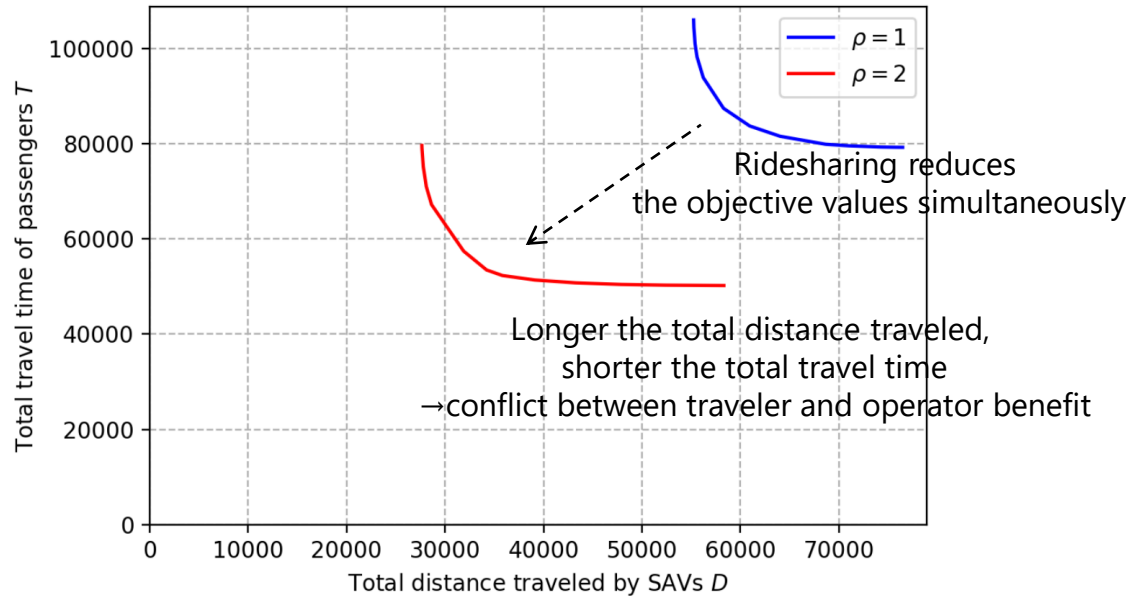
$$\kappa_i^{\min} \leq \kappa_i \leq \kappa_i^{\max} \quad \forall i$$

- DTA based on space-time network
- Consistent with standard DTA models
  - Conservation law of traffic
  - Free-flow speed, traffic capacity, jam density
- Important factors in SAV systems are captured
  - Traffic congestion
  - Empty vehicles' travel
  - Detour due to ridesharing
  - Waiting time of passengers



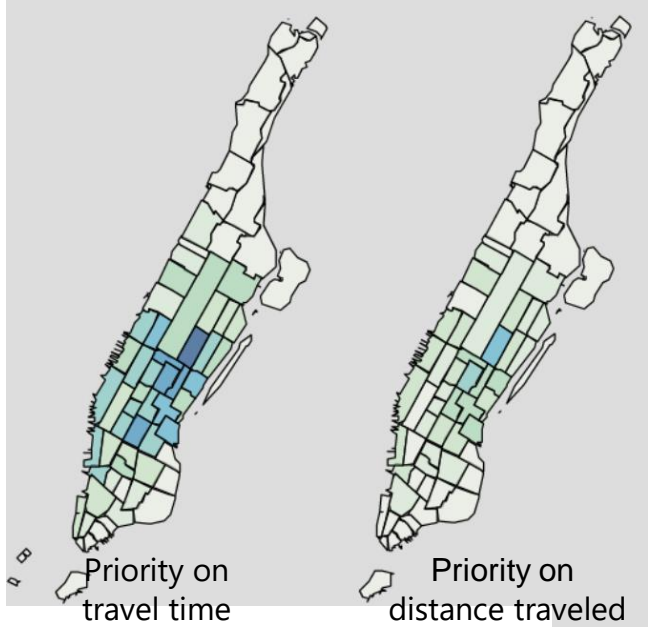
passenger demand

- NYC taxi data
  - 1 hour during morning peak
  - Total passenger demand: 17,998
- Derive optimal SAV system that serve this demand

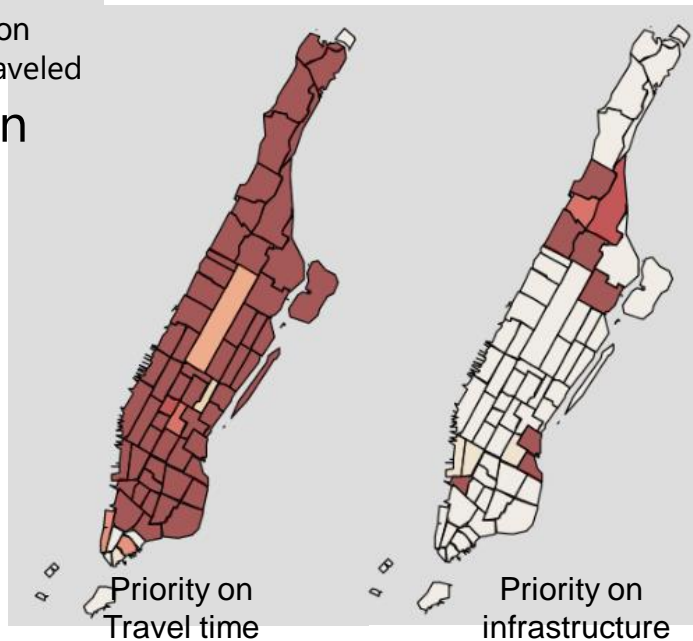


- Reasonable results
  - Trade-offs
  - Benefit of ridesharing
  - Operation patterns
- Consistent to some of the existing works based on detailed models





SAV flow distribution



Infrastructure requirement

- Reasonable results
  - Trade-offs
  - Benefit of ridesharing
  - Operation patterns
- Consistent to some of the existing works based on detailed models