

# Activity-based dynamic traffic assignment on regional networks and aggregated traffic models

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# Introduction to MFD-based models

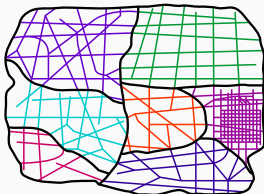
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# Scaling city into regional networks

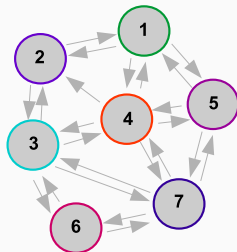
Urban network



Partitioning



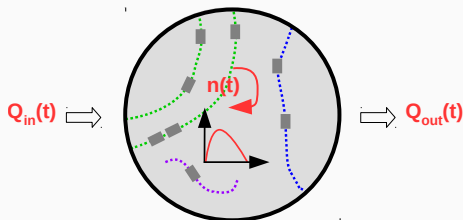
Regional network



\* Saeedmanesh and Geroliminis 2016, 2017; Lopez et al., 2017; Ambuhl et al. (2019); Batista et al. (in prep.).

# Aggregated traffic models based on the MFD

State variable:  $n(t)$  – accumulation – number of circulating vehicles in a region.



Flow conservation equation \*:

$$\frac{dn}{dt} = Q_{in}(t) - Q_{out}(t), t \geq 0 \quad (1)$$

$Q_{in}(t)$ : inflow [veh/s]

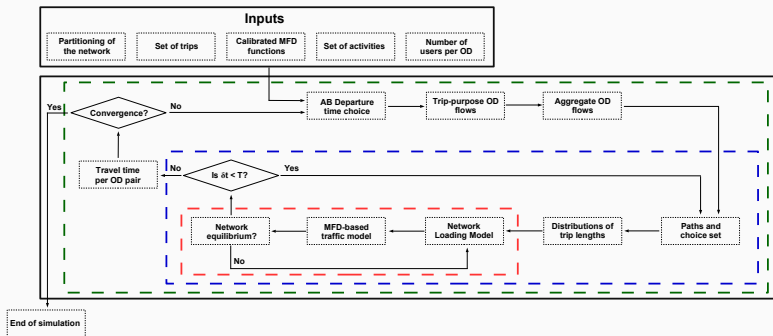
$Q_{out}(t)$ : outflow [veh/s]

\* Mariotte, G. and Leclercq, L. (2019), Flow exchanges in multi-reservoir systems with spillbacks. Transportation Research Part B: Methodological, 101:245–267, <https://dx.doi.org/10.1016/j.trb.2019.02.014>.

# **Activity-based DTA for regional networks and MFD models**

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# General framework



## **Activity-based and Departure time choice**

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# Utility-based DTA

The overall dis-utility of a user  $n$  doing an activity  $a$  knowing the departure time  $\tau$ , transportation mode  $m$  and path  $p$  is:

$$U_n^{OD}(\tau, m, p) = \max_{\tau, m, r} (U_n^T(\tau, m, p) + U_n^A(\tau)), \forall n \in N \wedge \forall (O, D) \in W \quad (2)$$

where  $O$  and  $D$  represent the Origin and Destination regions, respectively;  $N$  is the total number of users traveling on the OD pair; and  $W$  is the set of all OD pairs.

This network equilibrium can be formulated as a complementary problem:

$$\begin{cases} N(\tau, m, p) \cdot (U_n(\tau, m, p) - U^*) = 0 \\ N(\tau, m, p) \geq 0, U_n(\tau, m, p) - U^* \leq 0, \forall \tau, m, p \end{cases}$$

where  $U^*$  is the maximum dis-utility.



# Dis-utilities of traveling and performing an activity

The dis-utility of traveling  $U_n^T(\tau, m, p)$  is:

$$U_n^T(\tau, m, p) = \alpha_a^{OD} \cdot \overline{TT}^{OD} + \beta_a^{OD} \cdot EA + \gamma_a^{OD} \cdot LA \quad (3)$$

where  $\alpha_a^{OD}$ ,  $\beta_a^{OD}$  and  $\gamma_a^{OD}$  are the cost of traveling, early arrival and late arrival, respectively;  $EA$  is the scheduling delay;  $LA$  is the penalty of late arrival; and  $\overline{TT}^{OD}$  is the average travel time of the regional OD pair.

The dis-utility of performing an activity  $U_n^A(\tau)$  (Cantelmo and Viti, 2018; 2019) is:

$$U_n^A(\tau, t_a^i, t_a^f) = \int_{t_a^{i+1}}^{t_a^f} U_n^A(t') \cdot \left( \frac{1}{(t' - t_a^i)} \right)^G \cdot dt' \quad (4)$$

where  $G \in [0, 1]$  is an hyper-parameter of the model;  $t_a^i$  and  $t_a^f$  represent the starting and ending times of the activity. The dis-utility  $U_n^A(t')$  is given in Ettema and Timmermans (2003).

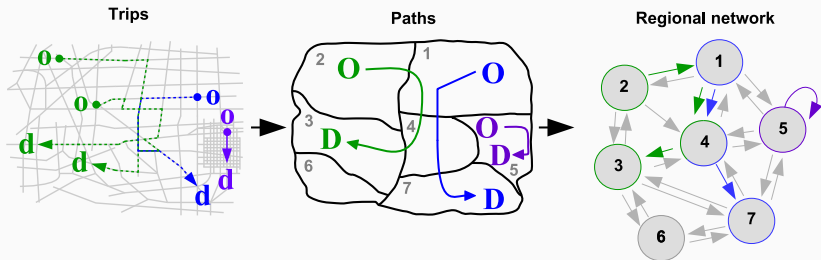
Cantelmo, G. and Viti, F. (2019), *A utility-based dynamic demand estimation model that explicitly accounts for activity scheduling and duration*, Transportation Research Part A, 114, 303-320, <https://doi.org/10.1016/j.tra.2018.01.039>.

Cantelmo, G. and Viti, F. (2019), *Incorporating activity duration and scheduling utility into equilibrium-based Dynamic Traffic Assignment*, Transportation Research Part B, 126, 365-390, <https://doi.org/10.1016/j.trb.2018.08.006>.

## **UE on regional networks**

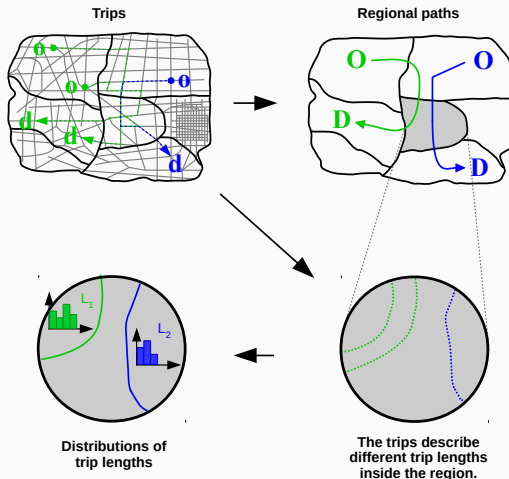
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# How to define paths on regional networks?



S. F. A. Batista, M. Seppacher and L. Leclercq (2021). *On the identification and characterization of paths on regional networks for MFD-based applications*, Transportation Research Part C: Emerging Technologies, 127, 102953, <https://doi.org/10.1016/j.trc.2020.102953>.

# How to characterize the regional paths?

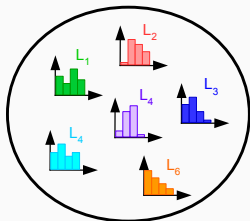


S. F. A. Batista, L. Leclercq and N. Geroliminis (2019). *Estimation of regional trip length distributions for the calibration of the aggregated network traffic models*, Transportation Research Part B, 122, 192-217, <https://doi.org/10.1016/j.trb.2019.02.009>.

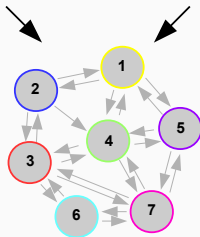
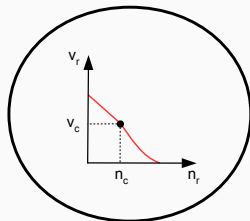
S. F. A. Batista, L. Leclercq and M. Menéndez (2021). *Dynamic Traffic Assignment for regional networks with traffic-dependent trip lengths and regional paths*, Transportation Research Part C: Emerging Technologies, 127, 103076, <https://doi.org/10.1016/j.trc.2021.103076>.

# How to define the regional network equilibrium?

Distributions of trip lengths for the regional paths crossing the region.



Traffic dynamics inside the regions: MFD.



# Travel time of a path in a regional network

The travel time  $TT_p^{OD}$  of a path is:

$$TT_p^{OD} = \sum_{r \in X} \left( \frac{L_{rp}}{v_r(n_r)} \right) \delta_{rp}, \forall p \in \Omega^{OD} \wedge \forall (O, D) \in W \quad (5)$$

The travel time  $TT_p^{OD}$  depends on:

- the sets of trip lengths  $\{L_{rp}\}$  for all regions  $r$  that define path  $p$ .
- the speed-MFD  $v_r(n_r)$  inside region  $r$  that defines path  $p$ .

DUE:

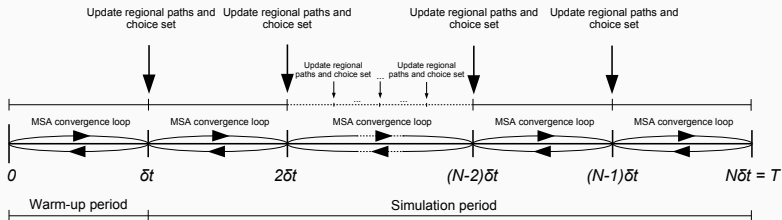
$$U_p^{OD} = \sum_{r \in X} \left( \frac{\bar{L}_{rp}}{\bar{v}_r} \right) \delta_{rp}, \forall p \in \Omega^{OD} \wedge \forall (O, D) \in W \quad (6)$$

SUE:

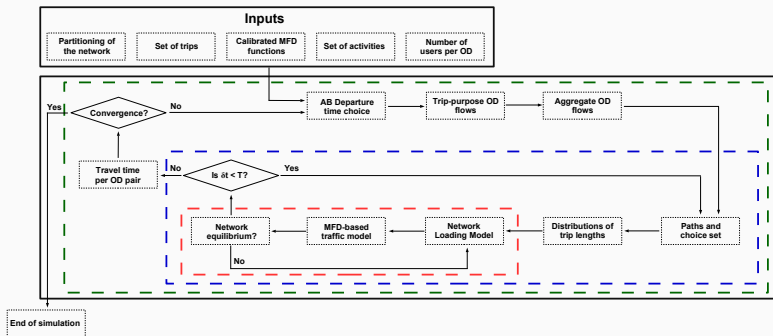
$$U_p^{OD} = \sum_{r \in X} \left( \frac{\bar{L}_{rp}}{\bar{v}_r} + \frac{L_{rp}}{\bar{v}_r} - \frac{\bar{L}_{rp} v_r}{\bar{v}_r^2} \right) \delta_{rp}, \forall p \in \Omega^{OD} \wedge \forall (O, D) \in W \quad (7)$$

S. F. A. Batista and L. Leclercq (2019). *Regional dynamic traffic assignment framework for macroscopic fundamental diagram multi-regions models*, Transportation Science, 53 (6), 1563-1590, <https://doi.org/10.1287/trsc.2019.0921>.

# Quasi-static approach to calculate the network equilibrium



# General framework: an overview

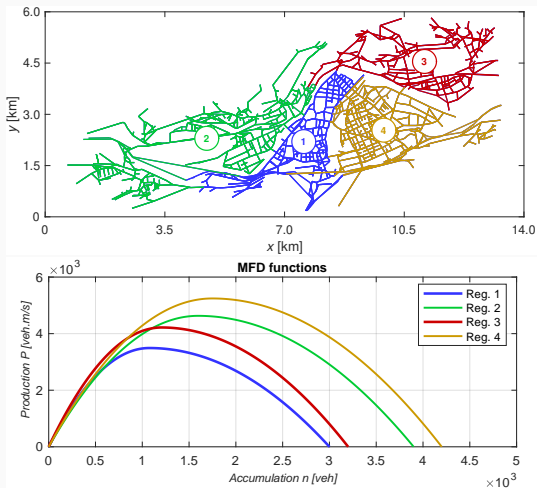




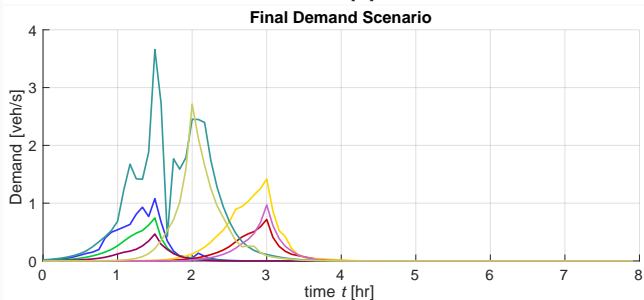
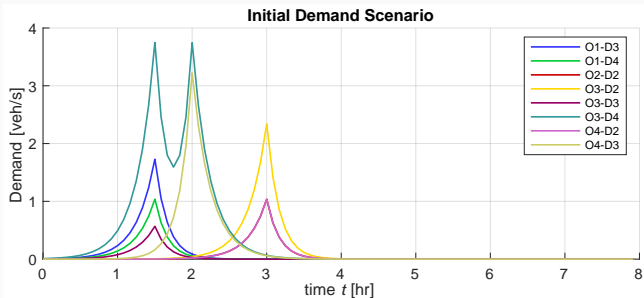
## Preliminary results

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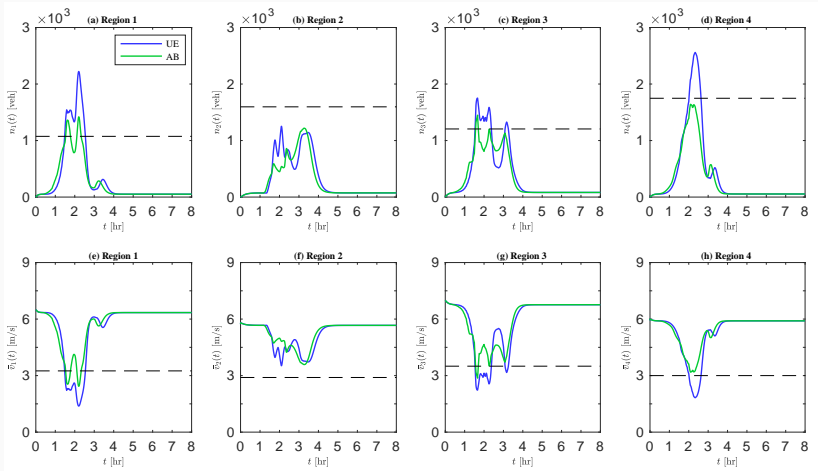
# Test network and MFD functions



# Demand scenario



# Accumulations and mean speeds in the regions



# Outline

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# Outline and future research directions

In this work, we:

- designed an Utility-based Dynamic Traffic Assignment model (which includes departure time and path choice) for regional networks and aggregated traffic models based on the MFD;
- discussed an example of application on the network of Innsbruck (Austria), partitioned into 4 regions, and considering three activities home-work;
- the dynamic choice of departure time flattens congestion around the peak hours.

As the next steps, we will:

- design a framework that does the departure time, mode and path choice simultaneously and propose a solution algorithm;
- introduce more realistic utility functions able to reproduce more complex mobility patterns;
- analyze the effect of special events on traffic patterns;
- show and discuss the importance of this activity-based DTA and MFD framework for applications of congestion pricing, environmental pricing and route guidance and perimeter control.

Thank you for your attention.

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